

# Rencontre CINES—chercheurs en chimie

## Thermodynamic modeling assisted by massive first principles calculations

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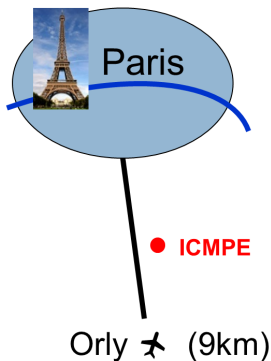
CINES, Montpellier, Septembre 2018



# ICMPE: Institute of Chemistry & Materials Science, Paris-East



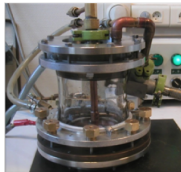
≈ 120 permanents + 50 non-permanents



# ICMPE: research on materials science

**Synthesis, Structural and chemical characterization**  
**XRD, EPMA, SEM-FEG-EBSD, ICP-OES, TDS, ATG, PPMS,...**

Ball-milling, SPS, melt spinning, induction and arc melting...



**Multi-scale calculations**

5 researchers, 3 PhDs, 4 workstations, no assist

GENCI since 2009: 1.400.000 h/year in 2018

# Multi-scale calculations

## computation of phase diagram?

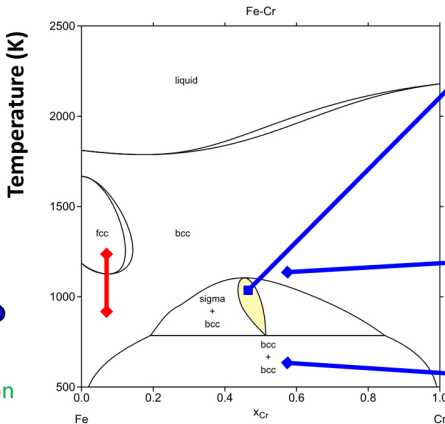
Calphad

Entropy?

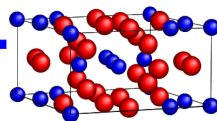


BWA,  
CVM

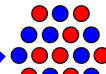
Phonon



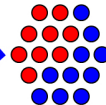
Enthalpy?



DFT, CEF



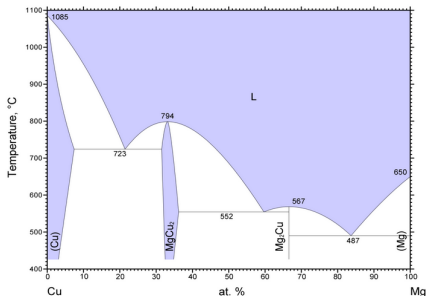
CEM,  
SQS



# Enthalpy of formation

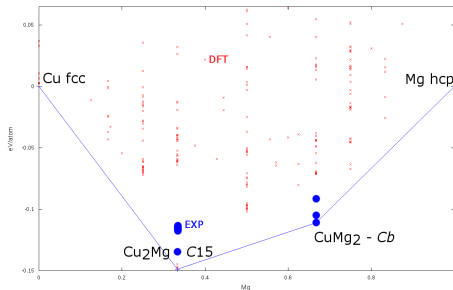
## Ex: Cu–Mg system

### phase diagram



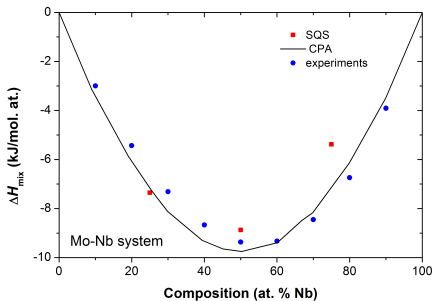
[1] DFT from AFLOW database

### calculation of heats of formation



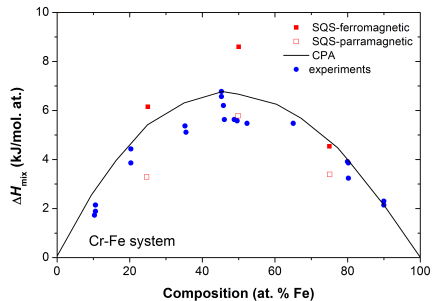
# Enthalpy of mixing

Ex: Mo–Nb (*bcc*):



[2] Jiang *et al.*, Phys Rev B 69 (2004)

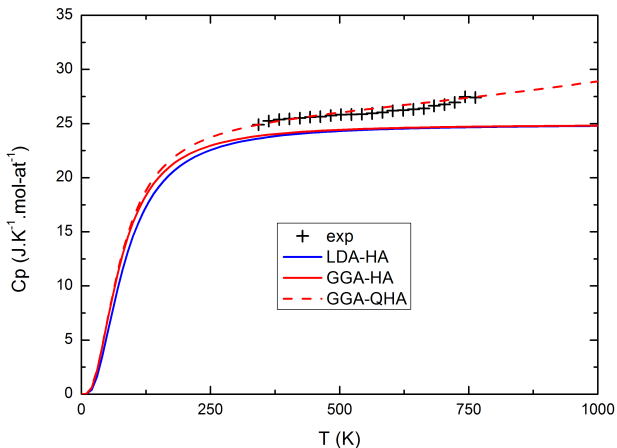
Ex: Cr–Fe (*bcc*):



$$F(T \neq 0)$$

Ex: Laves  $C15-Cu_2Mg$

Phonon calculation in harmonic, quasi-harmonic approximation:



# Calculation methods

- DFT PAW : VASP 5.4 (GGA, meta-GGA, mBJ)
- Phonopy 1.13 (Supercell approach)
- ATAT / MCSQS (CEM, SQS)



# Contents

Introduction

Non-stoichiometry in intermetallics

Thermoelectrics compounds

Ground state map of  $M-H$

Outlooks & Conclusions

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Introduction

**Non-stoichiometry in intermetallics**

Phase diagram with the Calphad method

Topologically Closed-pack phases

From binary to quaternary systems

Thermoelectrics compounds

Ground state map of  $M-H$

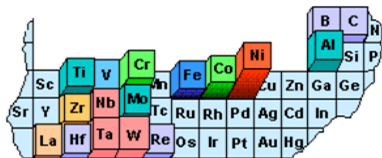
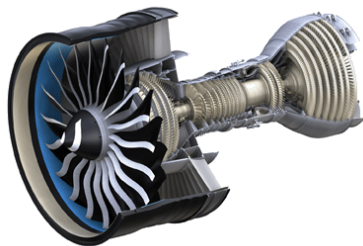
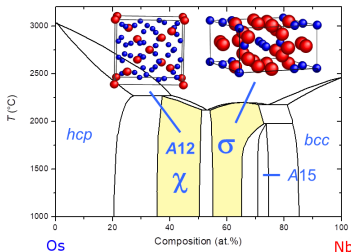
Outlooks & Conclusions

# Non-stoichiometry of complex intermetallics

In **superalloys**, (e.g. Ni-based) refractory bcc element is added:

- improve the creep resistance at high temperature
- precipitation of brittle IMC phases

Ex: Os–Nb phase diagram

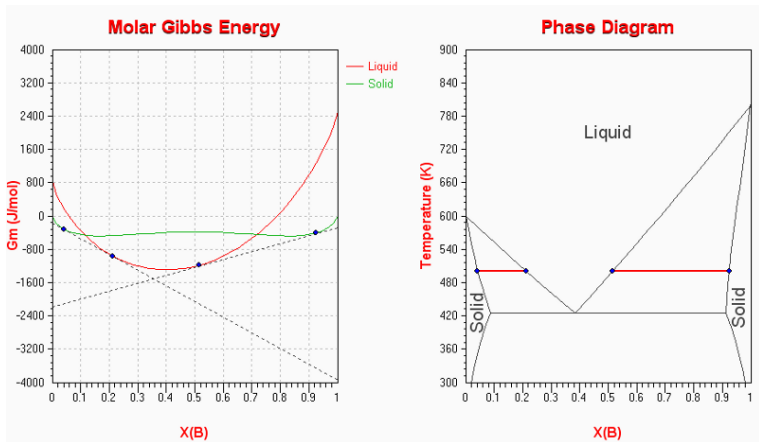


How can we predict IMC precipitation?

# Modeling of phase diagram

The **Calphad** method (*CAL*culat*ion* of *PH*ase *D*iagram) :

- based on Gibbs energies  $G^\varphi(x, T, P) = H - T \cdot S$
- phases  $\varphi_i$  in equilibrium if  $\mu_i = \left( \frac{\partial G}{\partial x_i} \right)_{P, T}$



# Thermodynamic modeling with Calphad

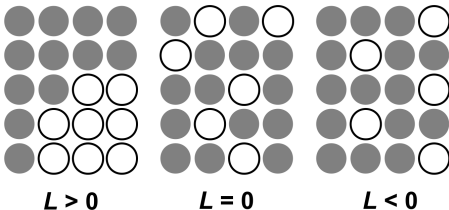
Using the **Compound Energy Formalism** (CEF):

$$G^\varphi = \text{srf} G^\varphi + \text{cnf} G^\varphi + \text{ex} G^\varphi + \text{phy} G^\varphi$$

[3] B. Sundman and B. J. Ågren, J. Phys. Chem. Solids 42 (1981) 297.

(i) description of a solid solution (ex:  $A - B$ ) :

- $\text{srf} G^\varphi = x_A G_A^\varphi + x_B G_B^\varphi$
- $\text{cnf} G^\varphi = -T \cdot \text{cnf} S^\varphi = -RT(x_A \ln x_A + x_B \ln x_B)$
- $\text{ex} G^\varphi = x_A x_B L_{AB}$  , où  $L_{AB} = \sum_{i=0}^n {}^i L_{A,B}^\varphi (x_A - x_B)^i$

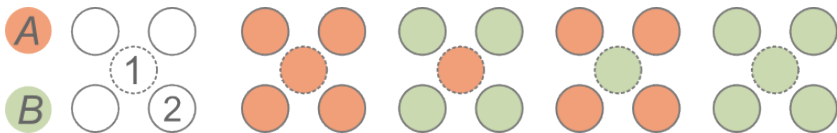


# Thermodynamic modeling with Calphad

(ii) description of a **non-stoichiometric compounds** in (CEF)

The  ${}^{\text{srf}}G^\varphi$  is expressed regarding the crystallography of the  $\varphi$  phase.

As an example, the compound  $AB$  described by a full substitution model  $(A, B) : (A, B)_1$



$${}^{\text{srf}}G = y_A^1 y_A^2 G_{A:A}^0 + y_A^1 y_B^2 G_{A:B}^0 + y_B^1 y_A^2 G_{B:A}^0 + y_B^1 y_B^2 G_{B:B}^0$$

Where each  $G^0 \simeq \Delta H_f$  could be expressed by DFT.

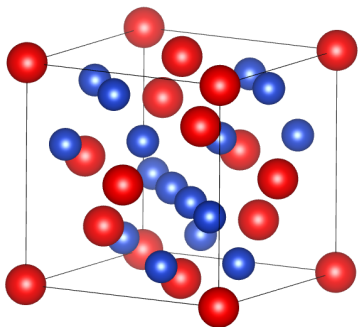
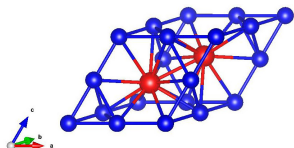
# An example: the Laves phase $\text{Cu}_2\text{Mg}$

## Crystal structure:

Strukturbericht:  $C15$ , Pearson:  $cF24$

Space group:  $Fd\bar{3}m$  (227, o1)

$a \simeq 7.05 \text{ \AA}$ , 6 atoms in the primitive cell



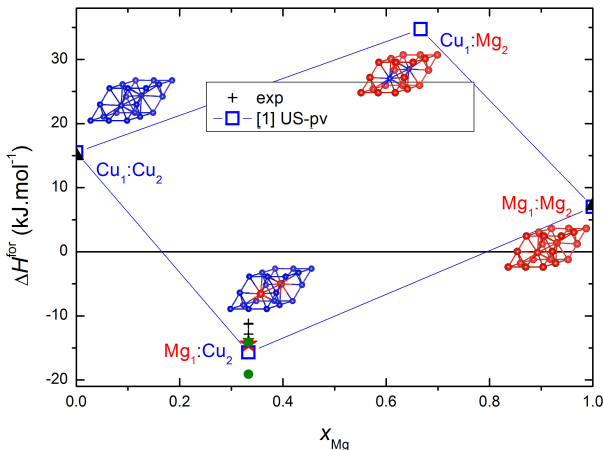
Site	Wyc	$x$	$y$	$z$	CN
Cu	$16d$	$\frac{5}{8} \frac{5}{8}$	$\frac{5}{8} \frac{5}{8}$	$\frac{5}{8} \frac{5}{8}$	12
Mg	$8a$	0	0	0	16

⇒ **DFT calculation of every end-members**

$C15$  : 2 sites,  $2^2=4$  ordered binary configurations in the CEF

# The Laves phase described by the $(Cu,Mg)_1:(Cu,Mg)_2$ model

Heat of formation of  $2^2=4$  end-members at 0 K



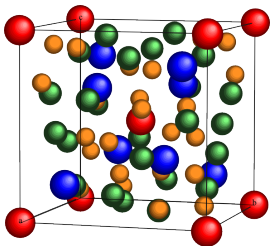


# More complex structures: the $\chi$ - and $\sigma$ -phase

## Crystal structure of the $\chi$ -phase

$\alpha$ -Mn,  $A12$ ,  $I\bar{4}3m$ , (217)

$a \simeq 9 \text{ \AA}$ , 58(29) atoms in 4 sites



Site	Wyc	$x$	$y$	$z$	CN
$A$	$2a$	0	0	0	16
$B$	$8c$	$\sim 0.32$	$x$	$x$	16
$C$	$24g_1$	$\sim 0.36$	$x$	$\sim 0.03$	13
$D$	$24g_2$	$\sim 0.09$	$x$	$\sim 0.28$	12

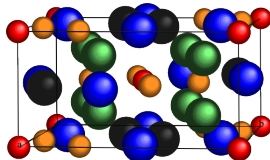
In a binary system:

$2^4=16$  different ordered configurations

## Crystal structure of the $\sigma$ -phases

$\sigma$ -CrFe,  $D8_b$ ,  $P4_2/mnm$  (136)

$a \simeq 9 \text{ \AA}$ ,  $c \simeq 5 \text{ \AA}$ , 30 atoms in 5 sites



Site	Wyc	$x$	$y$	$z$	CN
$A$	$2a$	0	0	0	12
$B$	$4f$	$\sim 0.39$	$x$	0	15
$C$	$8i_1$	$\sim 0.46$	$\sim 0.13$	0	14
$D$	$8i_2$	$\sim 0.74$	$\sim 0.07$	0	12
$E$	$8j$	$\sim 0.18$	$x$	$\sim 0.25$	14

In a binary system:

$2^5=32$  different ordered configurations

[4] Joubert *et al.*, Prog. Mater. Sci. 54 (2009)

[5] Joubert, Prog. Mater. Sci. 53 (2008)

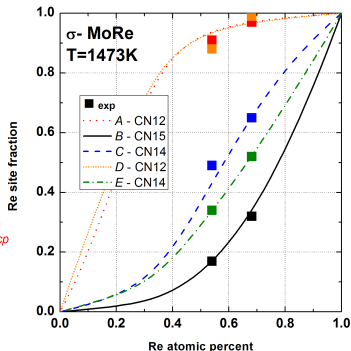
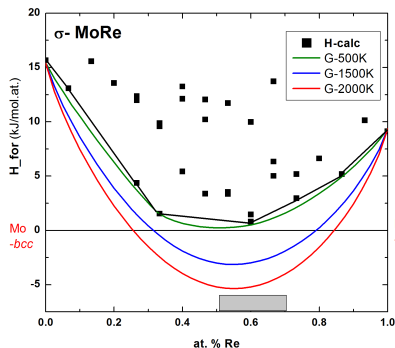
# The $\sigma$ -phase in a binary system, e.g. Mo-Re

- (1)  $\Delta H_{for}$  of every ordered compound:  $2^5 = 32$  configurations
- (2) Estimation of the Gibbs energy neglecting the interaction between atoms of same lattice (Bragg Williams – Gorsky approximation):

$$G^\sigma = \text{srf} G^\sigma + \text{cnf} G^\sigma + \cancel{\text{ex} G^\sigma} + \cancel{\text{phy} G^\sigma}$$

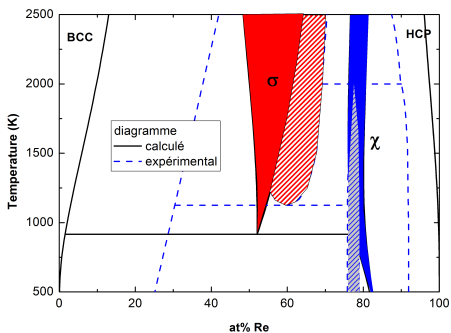
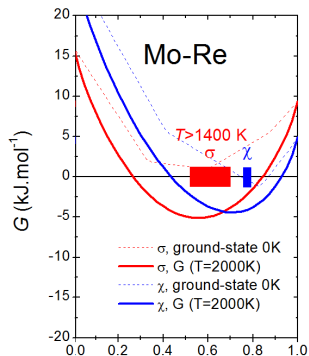
with  $\text{srf} G^\sigma = \sum_{ijklm=\text{Mo,Re}} [y_i^{(A)} y_j^{(B)} y_k^{(C)} y_l^{(D)} y_m^{(E)}] \times \Delta$  for  $H_{ijklm}^{0,\sigma}$

and  $\text{cnf} G^\sigma = -R \times T \sum_s a^{(s)} \sum_{i=\text{Mo,Re}} y_i^{(s)} \times \ln(y_i^{(s)})$



# An *ab initio* binary phase diagram

- (1)  $\Delta H_{for}$  of every ordered compound of both  $\chi$  and  $\sigma$ -phase
- (2) Estimation of the Gibbs energy in BWG approximation
- (3) phases diagram build from the common tangent rule



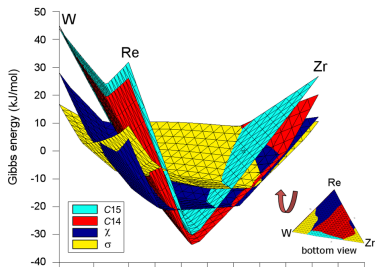
[6] Crivello *et al.* Inorg. Chem. (2013)

[7] Crivello *et al.* J. Phys.: Condens. Matter (2010)

# An ternary system? *e.g.* Re–W–Zr

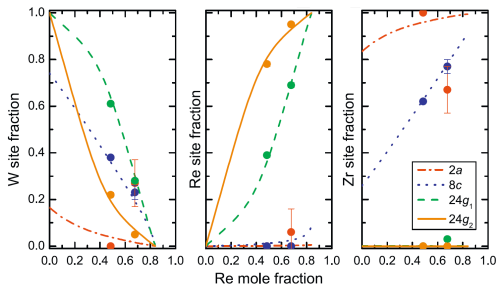
## Systematic calculations

- 4 phases:  $\chi$  ( $3^4 = 81$ ),  $\sigma$  ( $3^5 = 243$ ),  $C15$ ,  $C14$
- 3 solid solutions (fcc, bcc, hcp by SQS)



[8] Joubert, Crivello *et al.*, *Acta. Mater.* (2014)

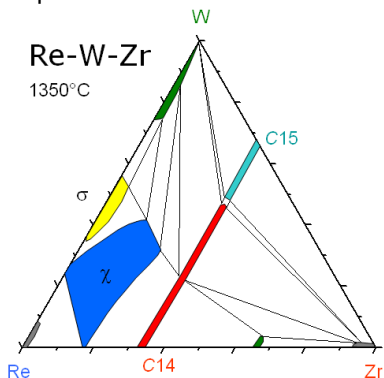
## Sites occupation in the $\chi$ -phase:



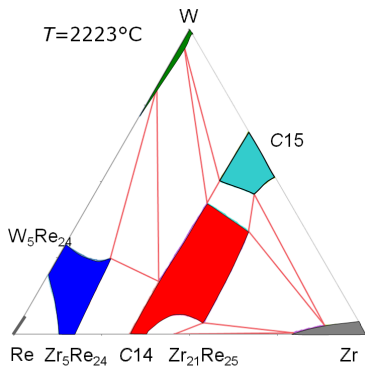
Experiment occupancies obtained by joint refinement on 2 diffraction sets of different contrast

# An *ab initio* ternary phase diagram

Experimental:



Computed with BWG approximation:



Similar agreement in other system: Mo-Ni-Re, Cr-Co-Re,...

[9] K. Yaqoob *et al.*, *Inorg. Chem.* (2012)

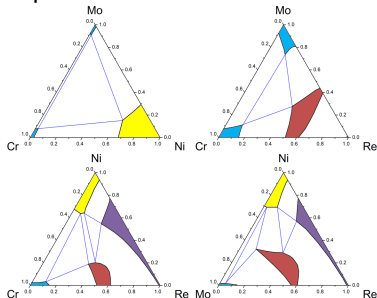
[10] Joubert, Crivello *et al.*, *Applied Sciences* (2015)

# Study of a quaternary system: Cr–Mo–Ni–Re

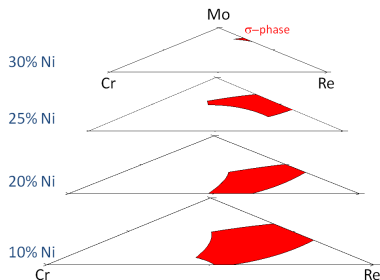
$4^5 = 1024$  configurations ordered in  $\sigma$  phase

Use of **ZenGen** code [11] Crivello *et al.*, Calphad (2015)

Experimental:



Computed with BWG approximation:



prediction of TCP phases precipitation

- BWA may works for complex IMC such as TCP ( $\chi$ ,  $\sigma$ , ...)
- not sufficient for more simple IMC such as Laves phases

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**Thermoelectrics compounds**

Fe<sub>2</sub>VAl for thermoelectric application

SQS and phonon calculations

Thermodynamic modeling

Ground state map of  $M-H$

Outlooks & Conclusions

# Temperature phase transition for thermoelectric applications

The **thermoelectric effect** is the conversion of temperature differences to electric voltage (and vice versa)

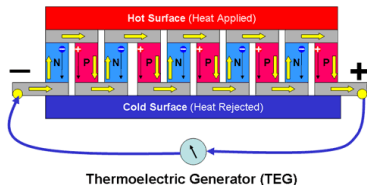
Evaluation of material with the **figure of merit**:  $ZT = \frac{\alpha^2 T}{\rho \lambda}$

Heusler type  $Fe_2VAl$ : potential candidate

- semi-metal, Pauli paramagnetic
- good electronic transport properties:  $\frac{\alpha^2}{\rho} = 5 \text{ mW m}^{-1} \text{ K}^{-2}$
- but thermal conductivity ( $\lambda$ ) is too large

Effect of temperature?

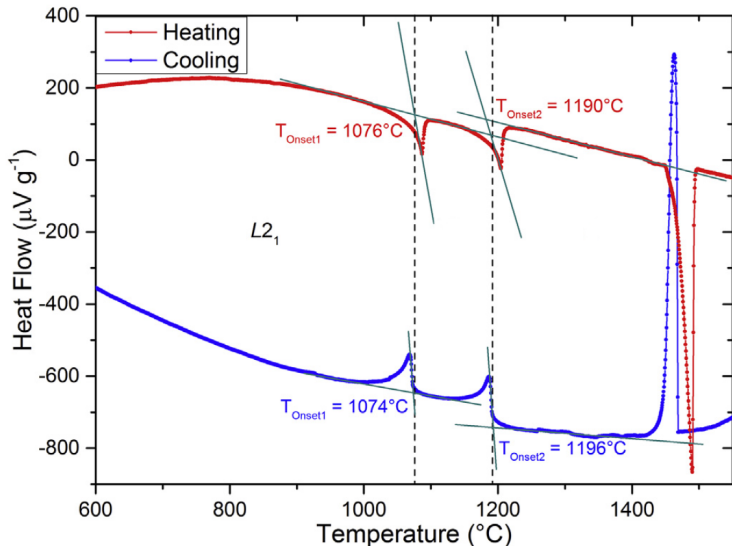
$Fe_2VAl$





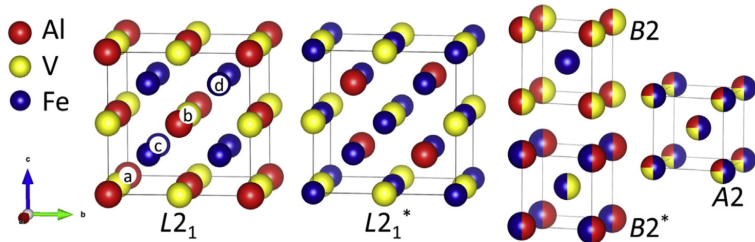
# $Fe_2VAl$ : phase transition

**experimental:** DTA heating and cooling scan



# Fe<sub>2</sub>VAl: phase transition

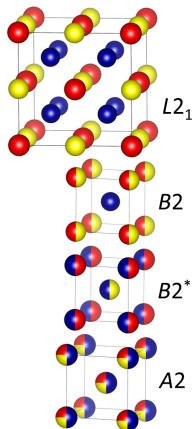
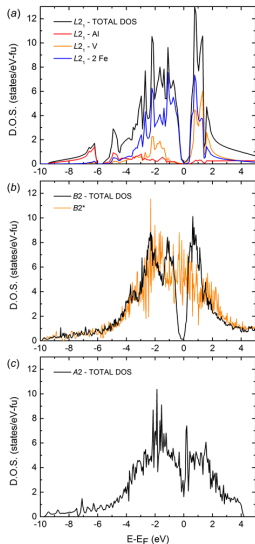
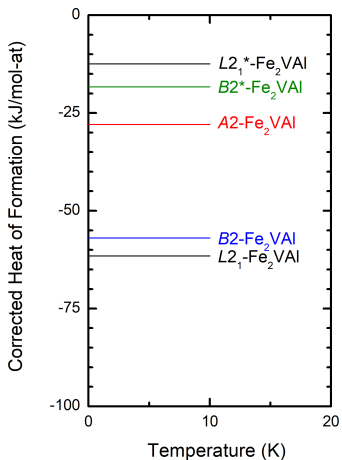
**theoretical work:** what is the most stable phase?  
with temperature dependence?



## two combined calculations

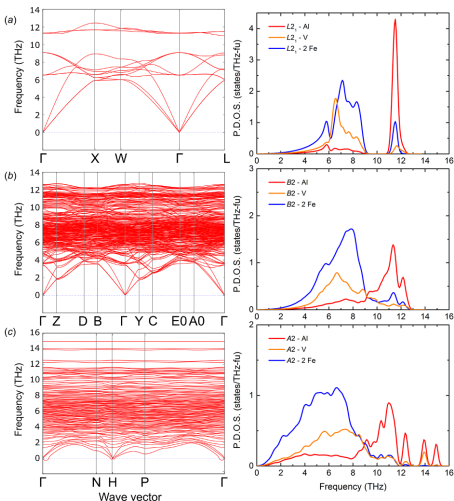
- SQS
- phonon

# Fe<sub>2</sub>VAl: SQS+DFT results at 0 K





# Fe<sub>2</sub>VAl: phonon calculations



Calculations done with Phonopy code in harmonic approximation [12] Togo, Oba, Tanaka, PRB 78 (2008)

- SQS-B2: 64 atoms, 112 displ.
- SQS-A2: 32 atoms, 191 displ.

From the phonon dispersion curves, Helmholtz free energy:

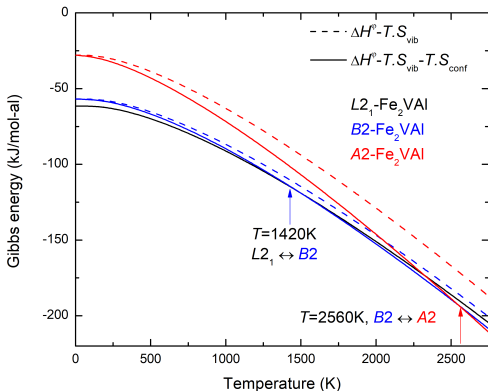
$$F(T) = \frac{1}{2} \sum_{\mathbf{q},s} \hbar\omega(\mathbf{q},s) + k_B T \sum_{\mathbf{q},s} \ln \left[ 1 - \exp \left( -\frac{\hbar\omega(\mathbf{q},s)}{k_B T} \right) \right]$$

$$S = - \left( \frac{\partial F}{\partial T} \right)_V ; \quad C_V = -T \left( \frac{\partial^2 F}{\partial T^2} \right)_V$$



# Fe<sub>2</sub>VAl: thermodynamic modeling

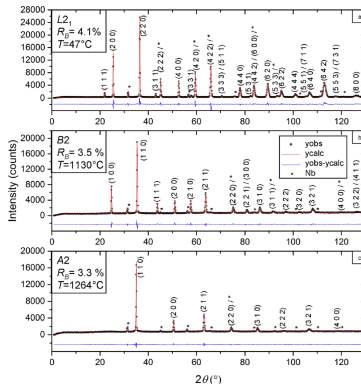
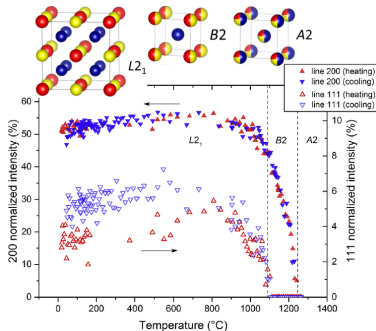
$$\Delta G^\varphi(x, T, P) = \Delta H - T \cdot \Delta S$$



⇒ Prediction of the phase transitions  $L2_1 \rightarrow B2 \rightarrow A2$

[13] Maier, Acta Mater. (2015)

# Fe<sub>2</sub>VAl: agreements



Neutron diffraction with temperature: order/disorder transitions

[14] Maier, Acta Mater. (2015)

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**Ground state map of  $M-H$**

The hydrogen economy

A ground state map design

Results on 31 systems

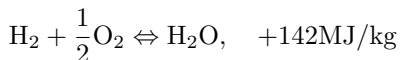
Vibrational contribution: application to isotopic effect

Outlooks & Conclusions

# The hydrogen economy

## Why hydrogen ?

- H is a renewable resource, very abundant (15% at. on Earth)
- H is a zero-emission fuel (when burned with oxygen)
- H is associated to a high exothermic reaction (in mass unit)



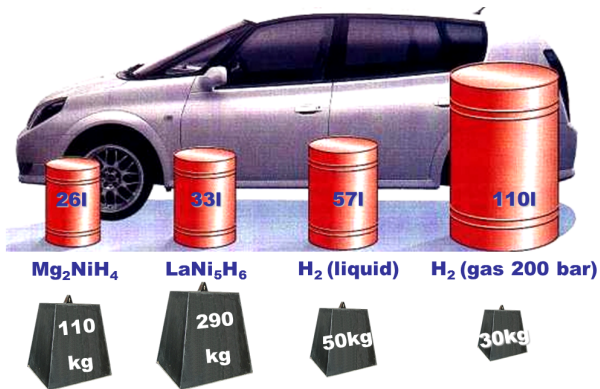
## What are its limitations?

- H needs to be produced
- H needs to be stored



# Hydrogen in the solid stored-state

4 liters of H is need to  
fed a fuel-cell for  
driving 400 km by car:



## Metallic hydride

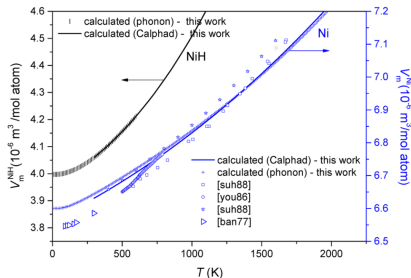
- presents high volumic density
- is safe (in opposition to the liquid or gas state)
- drives H with a tunable and reversible reaction

# A complete investigation: Ni-H system

A combined methodologies approaches based on **Calphad** modelling:

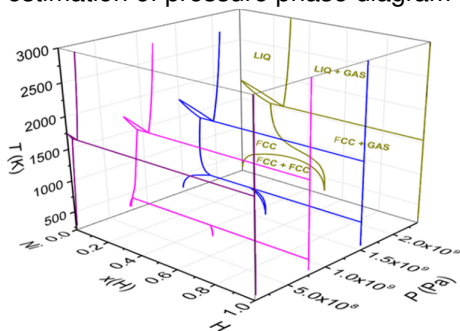
- DFT + CEM :  $\text{ex } G^{\varphi}$
- DFT + phonon QHA :  $V(T, P)$
- high pressure model:  $V(T, P) = x + y \ln \left( \frac{B}{P_0} \right)$

consistent set of volume equilibrium

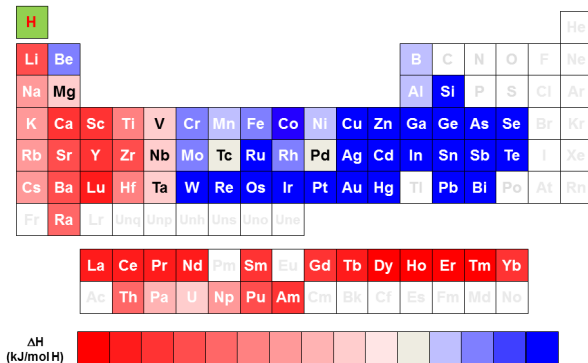


[15] Bourgeois *et al.*, J Phys Chem C, 119 (2015)

estimation of pressure phase diagram



# Binary metal hydrogen $M-H$ systems



Heat of formation of metallic hydride is governed by :

- the chemical nature of the host  $M$  element
- the crystal structure

# Ground state map of $M-H$

## A systematic/screening investigation by calculation

- 31 binary metal hydrogen  $M-H$  systems
- 30 crystal structures of hydrides

## Questions

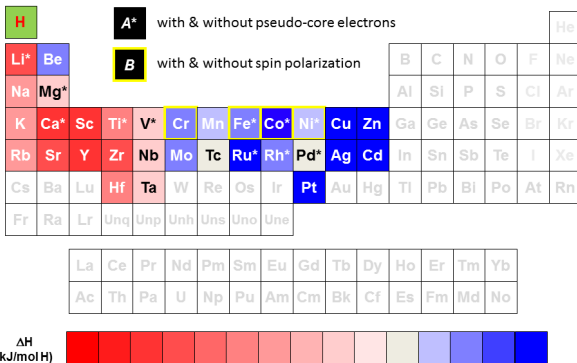
- Can we build a trustful thermodynamic database?
- May we can predict new hydride structure?
- What is the effect of the vibration?

### Application to the isotopic effect

## Methodology

- DFT at 0 K (PAW, VASP, GGA-PBE,  $E_{\text{cutoff}} = 800 \text{ eV}$   
 $\Rightarrow \Delta H_{\text{for}}(MH)^\varphi = E(MH)^\varphi - E(M)^{\text{SER}} - \frac{1}{2}E(\text{H}_2)^{\text{dimer}}$
- harmonic phonon calculation  $\Rightarrow$  ZPE,  $S_{\text{vib}}$

# 31 binary metal hydrogen $M-H$ systems



## Selection of $s$ - and $d$ -elements

covers a large variety of

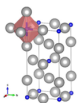
- crystal structures
- electronic structure types

# 30 crystal structures of binary hydrides

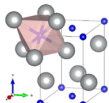
H/M	Proto.	P.S.	S.G.	Wyckoff P.	Site	M-H sys.
0.25	PdH <sub>0.25</sub>	tI8	$I4/mmm$ (139)	$M: 4c, 4e, H: 2a$	o	-
0.5	AuTe <sub>2</sub>	mC6	$C2/m$ (12)	$M: 4i, H: 2a$	o	V
0.5	TiO <sub>2</sub> -ana	tI12	$I4_1/amd$ (141)	$M: 8e, H: 4a$	o	Pd
0.5	CdI <sub>2</sub>	hP3	$P3m1$ (164)	$M: 2d, H: 1a$	o	Tc
0.5	Ta <sub>2</sub> H	oS6	$C222$ (21)	$M: 4k, H: 2a$	o	Ta
0.75	PdH <sub>0.75</sub>	tI8	$I4/mmm$ (139)	$M: 4c, 4e, H: 4d, 2b$	o	-
0.8	PdH <sub>0.8</sub>	tI10	$I4/m$ (87)	$M: 8h, 2a, H: 8h$	o	Pd
1	NbH <sub>0.95</sub>	oP8	$Pnnn$ (48)	$M: 4f, H: 2a, 2b$	te	Nb, Ti
1	PtS	tP4	$P4_2/mmc$ (131)	$M: 4c, H: 2a, 2b$	te	Zr, Ti
1	CsCl	cP2	$Pm\bar{3}m$ (221)	$M: 1a, H: 1b$	CN=4	$Na, K, Rb$
1	NaCl	cF8	$Fm\bar{3}m$ (225)	$M: 1a, H: 1b$	o	Li, Na, K, Rb, Ru, Co, Rh, Ni, Pd
1	ZnO	hP4	$P6_3mc$ (186)	$M: 2b, H: 2b$	te	Cu
1	CrB	oS8	$Cmcm$ (63)	$M: 4c, H: 4c$	CN=7	Cs
1	NiAs	hP2	$P6_3/mmc$ (194)	$M: 2c, H: 2a$	o	Cr, Mn, Co
1	anti-NiAs	hP2	$P6_3/mmc$ (194)	$M: 2a, H: 2c$	CN=6	-
1	FeH	hP14	$P6_3/mmc$ (194)	$M: 2c, 2a, H: 4f$	o	Fe
1	BN-b	hP2	$P6_3/mmc$ (194)	$M: 2c, H: 2d$	tr	-
2	ReB <sub>2</sub>	hP6	$P6_3/mmc$ (194)	$M: 2c, H: 4f$	te	-
2	TiO <sub>2</sub>	tP6	$P4_2/mnm$ (136)	$M: 2a, H: 4f$	tr	Mg
2	CaF <sub>2</sub>	cF12	$Fm\bar{3}m$ (225)	$M: 4a, H: 8c$	te	Sc, Y, Ti, Zr, Hf, V, Nb, Ta, Cr, Rh
2	PdF <sub>2</sub>	cP12	$Pa\bar{3}$ (205)	$M: 4a, H: 8c$	te	$Mg$
2	PbO <sub>2</sub>	oP12	$Pbcn$ (60)	$M: 4c, H: 8d$	tr	$Mg$
2	ThH <sub>2</sub>	tI6	$I4/mmm$ (139)	$M: 2a, H: 4d$	te	Ti, Zr, Hf
2	Co <sub>2</sub> Si	oP12	$Pnma$ (62)	$M: 4c, H: 4c$	te/CN=5	Ca, Sr
3	AuSb <sub>3</sub>	cl8	$Im\bar{3}m$ (229)	$M: 2a, H: 6b$	CN=2	-
3	BiF <sub>3</sub>	cF16	$Fm\bar{3}m$ (225)	$M: 4a, H: 4b, 8c$	o, te	-
3	ReB <sub>3</sub>	hP8	$P6_3/mmc$ (194)	$M: 2c, H: 2a, 4f$	o, te	-
3	HoD <sub>3</sub>	hP24	$P3c1$ (165)	$M: 6f, H: 12g, 4d, 2a$	tri/CN=3	Y
3	NaH <sub>3</sub>	hP8	$P6_3/mmc$ (194)	$M: 2c, H: 2d, 4f$	tr, te	-
3	Na <sub>3</sub> As	hP8	$P6_3/mmc$ (194)	$M: 2c, H: 2b, 4f$	tr, te	Gd

# 30 crystal structures of binary hydrides

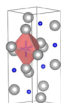
$H/M < 1$



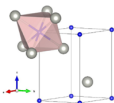
MoNi<sub>3</sub>



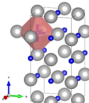
AuTe<sub>2</sub>



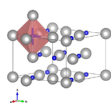
TiO<sub>2</sub>-ana



CdI<sub>2</sub>



MoNi<sub>3</sub>



MoNi<sub>4</sub>

$H/M = 1$



NbH



PtS



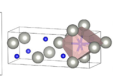
CsCl



NaCl



ZnO



CrB



NiAs



anti-NiAsBN



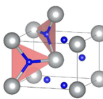
$H/M = 2$



BeH<sub>2</sub>



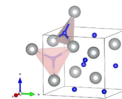
ReB<sub>2</sub>



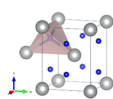
TiO<sub>2</sub>



CaF<sub>2</sub>



PbO<sub>2</sub>



ThH<sub>2</sub>

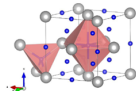


SiCo<sub>2</sub>

$H/M = 3$



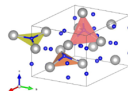
AuSb<sub>3</sub>



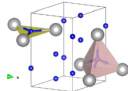
BiF<sub>3</sub>



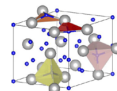
ReB<sub>3</sub>



HoD<sub>3</sub>



AsNa<sub>3</sub>

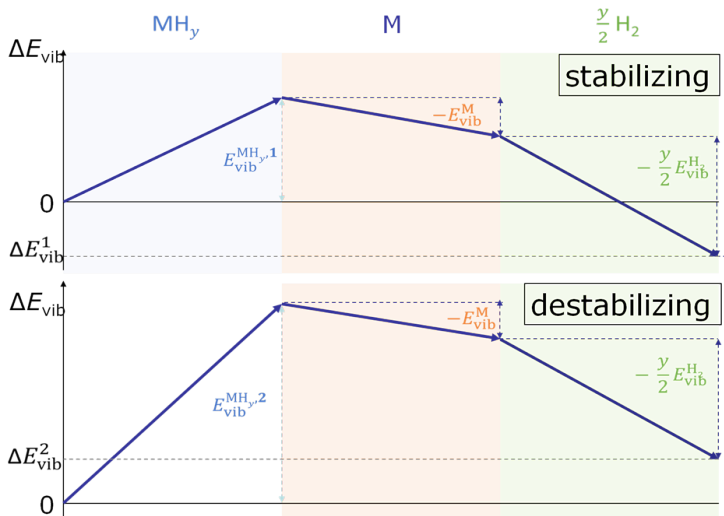


PCu<sub>3</sub>

# Strong importance of the ZPE contribution!

$$\Delta H_{\text{for}}^{\text{cor}}(MH_y) = \Delta H_{\text{for}}(MH_y) + \Delta E_{\text{vib}}$$

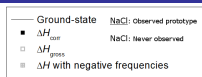
$$\Delta E_{\text{vib}} = E_{\text{vib}}(MH_y) - E_{\text{vib}}(M) - \frac{y}{2} E_{\text{vib}}(\text{H}_2^{\text{dimer}})$$



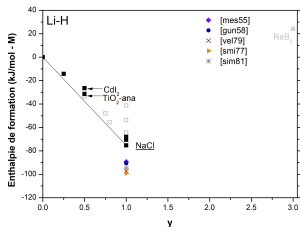


# Results: column 1, alkaline

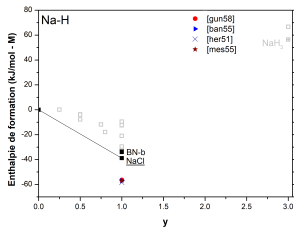
Li*	Be
Na	Mg*
K	Ca*
Rb	Sr



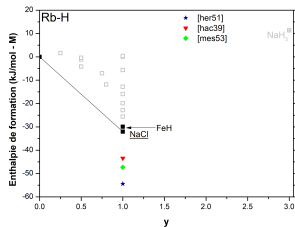
## Li-H



## Na-H



## Rb-H

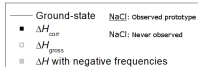


**agreements:** NaCl structure stable for the 4 alkali metal hydrides, with very unstable di-hydrides

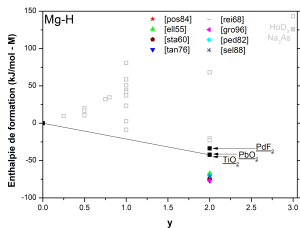
**chemical bonds:** ionic bond, strong charge transfer ( $\text{Li}^{+0.85}$ ,  $\text{Na}^{+0.78}$ ,  $\text{K}^{+0.75}$ ,  $\text{Rb}^{+0.74}$ ): decreasing with the increase of the period, associated with the decreased of the hydride stability

# Results: column 2, alkaline earths

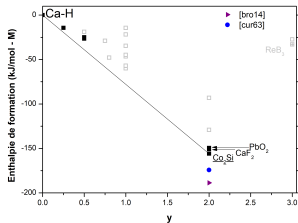
Li <sup>+</sup>	Be	
Na	Mg <sup>+</sup>	
K	Ca <sup>+</sup>	Sc
Rb	Sr	Y



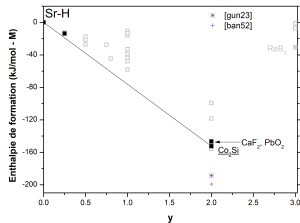
## Mg-H



## Ca-H



## Sr-H

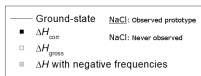


**agreements:** di-hydrides stable with correctly predicted structures, no-mono hydrides

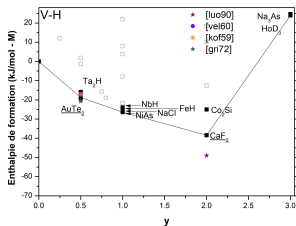
**chemical bonds:** important charge transfer ( $\text{Mg}^{+1.6}$ ,  $\text{Ca}^{+1.4}$ ,  $\text{Sr}^{+1.4}$ ), highly exothermic formation for Ca and Sr

# Results: column 5

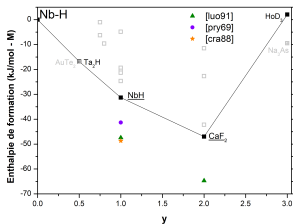
Ti <sup>+</sup>	V <sup>+</sup>	Cr
Zr	Nb	Mo
Hf	Ta	W



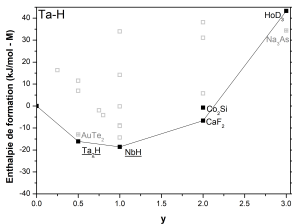
## V-H



## Nb-H



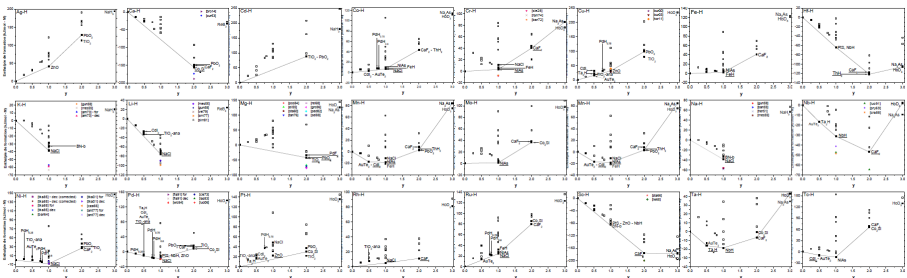
## Ta-H



**agreements:** all hydrides stable with correctly predicted structures  
 ( $MH_{0.5}$  stable only for  $M = V$ , no  $TaH_2$ )

**prediction:** monohydride  $VH$ ,  $TaH_2$  at 3 GPa

# A systematic/screening investigation

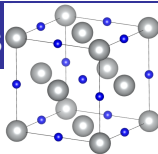


⇒ similar chemical properties for the hydrides formed with elements of the same column (chemical bonds, crystal structures,...)

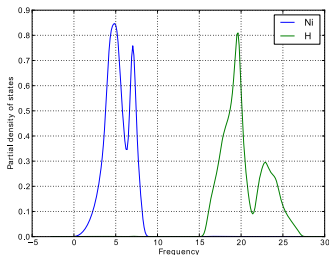
⇒ obtention of the ground state and assessment of the metastability

⇒ predicted structures in agreement with the experimental observations: prediction of higher hydrides  $TaH_2$  ( $CaF_2$ ),  $TcH$ ,  $PdH_2$  ( $Co_2Si$ ),  $ZrH_3$  ( $HoD_3$ ),  $AgH$  ( $ZnO$ ),  $TaH_2$  at 3 GPa

# Phonon calculation & thermodynamics



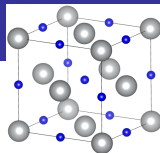
Ex: Results on NiH (B1, NaCl)



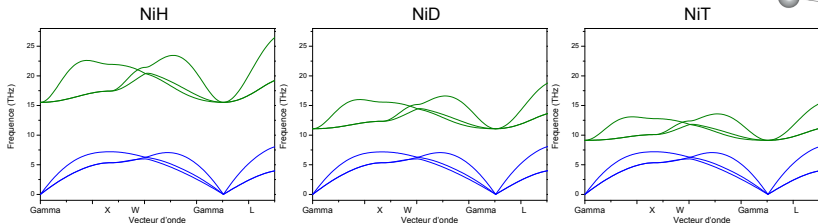
$$F(V_0, T) = \underbrace{\frac{1}{2} \sum_{\mathbf{q}, s} \hbar\omega(\mathbf{q}, s)}_{\text{ZPE}} + k_B T \sum_{\mathbf{q}, s} \ln \left[ 1 - \exp \left( -\frac{\hbar\omega(\mathbf{q}, s)}{k_B T} \right) \right]$$

**the ZPE contribution is not negligible for Metal-hydride systems!**

$$\omega \propto \frac{1}{\sqrt{m}} \Rightarrow \text{isotope effect}$$



## Ex: Results on NiH, NiD, NiT ( $B1$ , NaCl)



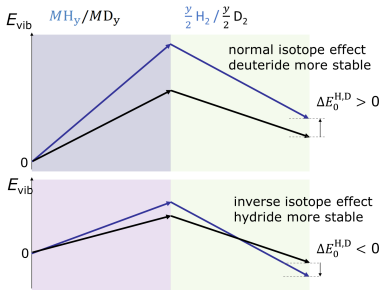
$$\Delta H_{\text{for}}^{\text{cor}}(\text{NiX}) = \Delta H_{\text{for}}(\text{NiX}) + \Delta E_{\text{vib}}$$

$$\text{where: } \Delta E_{\text{vib}} = E_{\text{vib}}(\text{MX}_y) - E_{\text{vib}}(\text{M}) - \frac{y}{2} E_{\text{vib}}(\text{X}_2^{\text{dimer}})$$

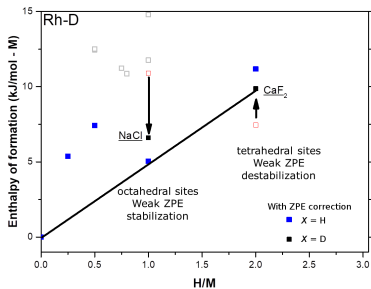
definition:

$$\Delta E^{\text{H,D}} = (E_{\text{vib}}(\text{MH}_y) - \frac{y}{2} E_{\text{vib}}(\text{H}_2)) - (E_{\text{vib}}(\text{MD}_y) - \frac{y}{2} E_{\text{vib}}(\text{D}_2))$$

# Isotope effect



⇒ prediction of normal or inverse stabilization

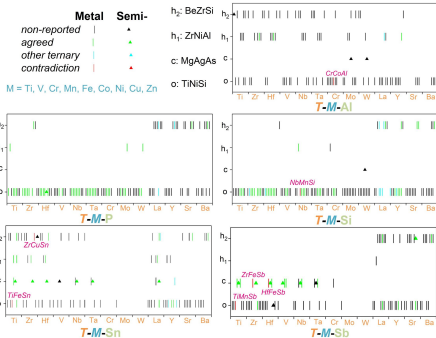
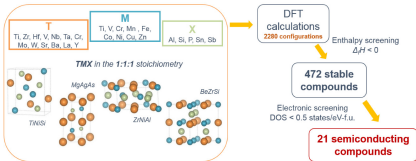


⇒ H/D: Modification of the ground state possible

[17] Bourgeois, Crivello *et al.*, J. Phys: Cond Mater 2018

# Outlook 1: Screening of new thermoelectric compounds

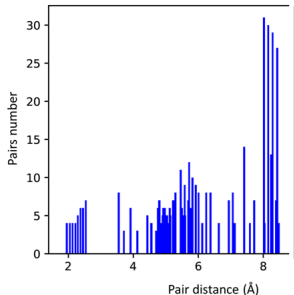
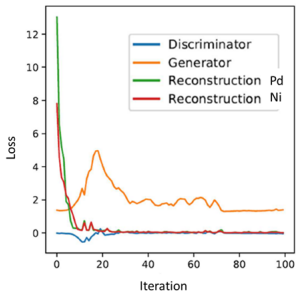
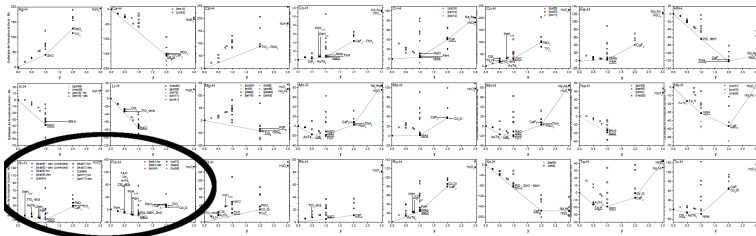
H																	He				
Li	Be															B	C	N	O	F	Ne
Na	Mg															Al	Si	P	S	Cl	Ar
K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr				
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe				
Cs	Ba		Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At	Rn				
Fr	Ra		Rf	Db	Sg	Bh	Hs	Mt	Ds	Rg	Cn	Nh	Fl	Mc	Lv	Ts	Og				
		La	Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu					
		Ac	Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr					



[18] Barreteau, Crivello *et al.*, J. Comput. Mater. 2019



# Outlook 2: Machine learning for metal hydrides?



# Conclusions

## Thermodynamic modeling assisted by massive first principles calculations

### Type of calculations

- large number of small DFT calculations:  $\sim 30$  atoms/cell
- phonon calculations: large number of asymmetric supercell
- magnetism for alloys: collinear and non-collinear
- oxides & thermoelectrics: use of meta-GGA and mBJ functionals

### Continuous Help in VASP needs: thanks the CINES Support

- help for choosing the NPAR and KPAR parameters
- help for number of nodes
- guide for typical errors

# Advert & Acknowledgments

<https://ai4mater-sci.sciencesconf.org/>

